

## **DETERMINING MONEY DEMAND** **AT PRICE FLUCTUATIONS IN THE MARKET**

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### **Abstract**

This article is devoted to ways of determining money demand and supply. It should be noted, that one of peculiarities of the economy of Uzbekistan is a slight dependence of the inflation rate from the change of money supply. Moreover, the article provides developed economic-mathematical model and the ways of stabilizing money issue while changing prices in the market. In addition, the article demonstrates the quantitative example of the demand for money issue while price fluctuations.

**Keywords:** demand, supply, inflation, money supply, money circulation, equilibrium, sustainability, price changes, money circulation velocity.

### **Introduction**

One of the peculiarities of the economy of Uzbekistan is a slight dependence of the inflation rates on the rates of the money supply change. This is justified by the fact that price changes are prior to money changes, i.e. prices are considered to be causative in relation to money. The main reason for the change of the overall price level are non-monetary inflation factors such as raising the level of pensions, allowances, salaries for government officials, gradual administrative release of prices on the energy resources, external economic factors (changes of exchange rates, oil prices in the world markets, etc.) and fiscal ones. The change of price level is resulting in changing of the money demand which is satisfied by banks

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through internal borrowings. However, inspiteofthefactthatmonetarypolicyhasafulfilling role, inflation processes at the end are supported by additional money issue in circulation. Tocurbtheinflation it is necessary to introduce a tight monetary policy, therefore it is advisable to forecast equilibrium demand and supply of the money issue while price fluctuations in the market.

### Model

It is known that money circulation is determined by the equation of I. Fisher [1]

$$MV = PQ(1)$$

where:  $M$  – moneysupply;  $V$  – moneycirculationvelocity;  $P$  – average price for goods and services;  $Q$  – physical amount of productive goods and services. The leftsideoftheequation(1) representsatotalvolumeofexpenditures of buyers (money supply) on purchasing production benefits. The right side of the equation (1) represents overall receipts of sellers of these benefits, in other words, it is demand on money.

If we rewrite the right side of the equation (1) in the form of the demand line  $D: P^D = k_1q + b_1$  and the left side in the form of the supply line  $S: P^S = k_2q + b_2$ , where –  $k_1$  and  $q$  – average price and the volume of goods and services in the demand line  $D$ ;  $b_1$  – demand for money for transaction expenditures;  $k_2$  and  $q$  – velocity of circulation and money supply (issue) in the supply line  $S$ ;  $b_2$  – share of other money aggregates in the money supply. If to take into account (1),

$$k_2q - P^S + b_2 = k_1q - P^D + b_1 \quad (2)$$

Changesoftheeconomic indicators depend on the scales of measuring thus they can be incomparable. Forexample, in(2)thevalueoftheindicatorofmoneyissuevolume  $P^D$  can be incomparable with the average indicator of the equilibrium price of supply of goods and services  $P^S$ . Thereforeitismoreconvenienttoconsidernot absolute changes of economic variables but relative ones [2].With their help it is possible to compare money markets and market of goods and services when the result is considered in the portions of units or per cents. Relativevalues are

convenient not only for measuring but also for comparison. Therefore equation (2) the ratio of the equilibrium of the money issue is to be determined.

Demand line D and supply line S of money are compared with the general form of equations:

$$\begin{cases} A_1q + B_1p + C_1 = 0 \\ A_2q + B_2p + C_2 = 0 \end{cases} \quad (3)$$

where,

$A_1, B_1, C_1$  and  $A_2, B_2, C_2$  – real (actual) numbers,

$$A_1 = K_1, B_1 = -1, C_1 = b_1 \text{ and } A_2 = K_2, B_2 = -1, C_2 = b_2$$

Solution of the equation system (3) can be determined by the matrix method

$$P = \left[ \begin{array}{c|c} C_1A_1 & A_1B_1 \\ \hline C_2A_2 & A_2B_2 \end{array} \right] = \frac{C_1A_2 - C_2A_1}{A_1B_2 - A_2B_1} \quad (4)$$

To determine the equilibrium coefficient of the money issue for forecasted period time  $t$  is introduced. [3]

If  $P$  – money supply then  $\frac{dP}{dt} = P'$  – will be the tendency of formulating money issue (derived money supply in time period), money supply will be functions of the stated values [4].

$$\text{Differentiating (4) by } t: \frac{dP}{dt} = \left[ \frac{C_1A_2 - C_2A_1}{A_1B_2 - A_2B_1} \right]' = 0,$$

as the derivative of some number or ration is equal to zero.

Transferring the right side of the equation (4) into the left side and recording as  $\frac{dP}{dt} = 0$  the following equation is developed:

$$\frac{dP}{dt} + P - \frac{C_1A_2 - C_2A_1}{A_1B_2 - A_2B_1} = 0,$$

where,

$A_1, A_2, B_1, B_2, C_1$  and  $C_2$  – real (actual) numbers. Indicating their relations for further calculations through  $F = \frac{C_1A_2 - C_2A_1}{A_1B_2 - A_2B_1}$ , the result of  $\frac{dP}{dt} + P - F = 0$  is achieved.

Hence the differential equation is developed:

$$\frac{dP}{P-F} = -dt.$$

Integrating last differential equation and then potentiating, we will get that  $P = Ce^{-t} + F$

Having applied the value  $F$  the following equation is developed:

$$P = C e^{-t} + \frac{C_1 A_2 - C_2 A_1}{A_1 B_2 - A_2 B_1}, \quad (5)$$

Then Cat initial conditions  $t_0 = 0$   $uP_0 = 1,00$  (or 100%) is calculated:

$$C = 1 - \frac{C_1 A_2 - C_2 A_1}{A_1 B_2 - A_2 B_1}.$$

Setting C in the final equation, the following equation is formulated”

$$P_t^* = \left[ 1 - \frac{C_1 A_2 - C_2 A_1}{A_1 B_2 - A_2 B_1} \right] e^{-t} + \frac{C_1 A_2 - C_2 A_1}{A_1 B_2 - A_2 B_1}, \quad (6)$$

where  $e = 2,7183$ ;  $t$  –forecasted time period.

Thus, to maintain equilibrium between the money demand and money supply it is necessary to change money supply according to the last formula (6).  $P_t^*$  is a relative value. Absolute or actual value of the forecasted money supply for time  $t$  ( $P_t^m$ ) is to be determined according to the formula

$$P_t^m = P_t^* * P_0 \quad (7)$$

where  $P_0$  –money supply at the beginning of the forecasted period.

One of the ways of calculating money ratios  $A_1, A_2, B_1, B_2, C_1$  and  $C_2$  lines of demand D and supply S is the method on the basis of marketing research for analyzed forecasted period of time to determine coordinates of the minimum and maximum values of  $(P_1^D, q_1^D)$  and  $(P_2^D, q_2^D)$  by demand  $(P_3^S, q_3^S)$  and  $(P_4^S, q_4^S)$  by supply.

From the analytical geometry it is known that the equation of solid lines of the demand D and supply S, passing through two points are recorded as it follows:

$$\frac{p - p_1}{p_2 - p_1} = \frac{q - q_1}{q_2 - q_1}; \quad \frac{p - p_3}{p_4 - p_3} = \frac{q - q_3}{q_4 - q_3},$$

After transformations these equations will look like:

$$\begin{cases} (p_2 - p_1)q - (q_2 - q_1)p + p_1 q_2 - q_1 p_2 = 0 \\ (p_4 - p_3)q - (q_4 - q_3)p + p_3 q_4 - q_3 p_4 = 0 \end{cases}$$

However, these solid lines of the demand and supply are similar to the equation of the solid lines (3). Being compared they look as it follows

$$\begin{cases} A_1 = p_2 - p_1, B_1 = -(q_2 - q_1), C_1 = p_1q_2 - q_1p_2 \\ A_2 = p_4 - p_3, B_1 = -(q_4 - q_3), C_1 = p_3q_4 - q_3p_4 \end{cases} \quad (8)$$

Thus, values  $A_1, A_2, B_1, B_2, C_1$  and  $C_2$  by formulas (8) and put their values in (6). Then for time  $t = t_1, t_2, \dots, t_n$   $P_t^*$  is determined and used it in (7) we are forecasting the value of money issue for the analyzed period.

This case can be evidenced by the example. On the basis of studying the conditions of the market of goods and services, marketing service unit has determined that monthly reduction of prices in the first quarter and its increase in the second quarter is supposed. In addition they defined that while price reduction on the forecasted first quarter by the demand:  $P_1^D = 0,98$  and  $P_2^D = 0,95$ ,  $q_1^D = 0,82$  and  $q_2^D = 0,90$ ; (9) by supply:  $P_3^S = 0,99$  and  $P_4^S = 1,07$ ,  $q_3^S = 1,18$  and  $q_4^S = 1,01$ .

And in forecasted second quarter while the price growth by demand:  $P_1^D = 0,99$  and  $P_2^D = 1,05$ ,  $q_1^D = 0,97$  and  $q_2^D = 0,88$ ; (10) by supply:  $P_3^S = 1,04$  and  $P_4^S = 1,07$ ,  $q_3^S = 1,08$  and  $q_4^S = 1,27$ .

It is necessary to determine the equilibrium coefficients of money issue change by month of the first and second quarter.

With this aim, first it is advisable to develop the demand and supply equation for the first quarter. We are detecting the values of  $A_1, B_1, C_1$  and  $A_2, B_2, C_2$  from formulas (8) at the price reduction (9): by demand:

$A_1 = -0,03$ ;  $B_1 = -0,08$ ;  $C_1 = 0,98 * 0,90 - 0,82 * 0,95 = 0,103$  or considering the equation of the demand line:  $-0,03q - 0,08p + 0,103 = 0$ ;  
by supply:  $A_2 = -0,02$ ;  $B_2 = 0,17$ ;  $C_2 = 0,99 * 1,01 - 1,18 * 0,97 = -0,145$ ;  
or considering the equation of the supply line:  $-0,02q + 0,17p - 0,1450 = 0$ .

Then, applying these values in formulas (6) we are determining an equilibrium coefficient of the money issue at price reduction. Relative starting time  $t_0 = 0$ , forecasted monthly time of the quarter  $t_1 = 1, t_2 = 2$  and  $t_3 = 3$ .

If  $t_0 = 0, P_0^* = 1,00$  or 100%, i.e. equal to the money supply at the starting point of  $P_0$ . If  $t_1 = 1$ , the equilibrium coefficient of the money issue in the first month of the quarter will be:

$$P_1^* = \left(1 - \frac{-0,103 * (-0,02) - (-0,145) * (-0,03)}{(-0,03) * 0,17 - (-0,02) * (-0,08)}\right) * 2,7183^{-1} + \frac{-0,00206 - 0,00435}{-0,0051 - 0,0016} = (1 - 0,9567) *$$

$0,3679 + 0,9567 = 0,97263$  or 97,263% from the starting point.

If  $t_2 = 2$ , the equilibrium coefficient of the money issue in the second month of the quarter will be:  $P_2^* = (1 - 0,9567) * 0,1353 + 0,9567 = 0,96256$  or 96,256%.

If  $t_3 = 3, P_3^* = 0,0433 * 0,04979 + 0,9567 = 0,958856$  or 95,8856%.

Then having determined  $P_3^m = P_3^* * P_0 = 0,958856 *$

$P_0$  for the beginning of these second quarter we will consider this coefficient as 100% or for the initial equilibrium coefficient of the starting point of the second quarter.

We are developing the equation of the demand and supply using the formulas (8) and the data (10):

by demand:  $A_1 = 0,04; B_1 = 0,09; C_1 = 1,01 * 0,88 - 0,97 * 1,05 = -0,1297$  or we are having the equation of the demand line  $0,04q + 0,09p - 0,1297 = 0$ ;

by supply:  $A_2 = -0,02; B_2 = 0,17; C_2 = 0,99 * 1,01 - 1,18 * 0,97 = -0,145$  or we are having the equation of the supply line  $0,03q - 0,19p + 0,1652 = 0$ .

Applying these values in formulas (6), the equilibrium coefficient of the money issue while the price growth can be determined.

If  $t_0 = 0, P_0^* = 1,00$  or 100%, i.e. equal to the money supply at the starting point  $0,95699P_0$ .

If  $t_1 = 1$ , the equilibrium coefficient of the money issue for the first month of the second quarter is calculated:

$$P_1^* = \left(1 - \frac{(-0,1297)*0,03 - 0,1652*0,04}{0,04*(-0,19) - 0,03*0,09}\right) * 2,7193^{-1} + \frac{-0,003891 - 0,006608}{-0,0076 - 0,0027} = -0,0071 + 1,0193 = 1,0122 \text{ or } 101,22\%$$

In addition, calculations are made for the second  $t_2$  and third  $t_3$  months of the second quarter:

$$P_2^* = -0,0193 * 0,1353 + 1,0193 = 1,0167 \text{ or } 101,67\%$$

$$P_3^* = -0,0193 * 0,04979 + 1,0193 = 1,0183 \text{ or } 101,83\%$$

Absolute or real (actual) value of the forecasted money supply by months of the first and second quarter can be determined according to the following formula (7). As a result of calculations the following values are received for the first quarter:  $EMD_1^1 = 0,96256P_0$ ;  $EMD_2^1 = 0,96256P_0$ ,  $EMD_3^1 = 0,958856P_0$ , for the second quarter:  $EMD_1^2 = 1,0122 * 0,958856 * P_0$ ;  $EMD_2^2 = 1,0167 * 0,958856P_0$ ,  $EMD_3^2 = 1,0183 * 0,958856P_0$ . Here  $EMD_t^k$  – (t – number of month and k – number of quarter) means forecasted value of the money issue of the appropriate period.

## Conclusion

It should be noted that in spite of intensive development of various means of implementing non-cash settlements, cash circulation remains one of the most important spheres of the modern economy. Some specialists think that dynamic development of non-cash payments in the sphere of retail payments is being currently observed all over the world. As a result, the illusion that the era of “cash” is coming to the end appears. Some experts already consider cash as outdated means of payment. However, as the practice illustrates, the amount of cash money in circulation is constantly increasing [7].

In modern economy in many countries cash money circulation comprises of the smaller part of money circulation but has a significant functional importance. It is justified that final realization of produced goods and services is implemented and the compliance of supply and demand is checked in the sphere of the cash money circulation. Purchasing power parity of the national currency mainly depends on the condition of the cash money circulation.

This is also justified by the great attention paid to the modernization and development of cash circulation, raising efficiency of cash circulation in most countries of the world. In this aspect, improving the organization and regulation of money circulation play an important in predicting money issues.

In conclusion, it should be noted that the determination of demand for money if prices are fluctuating are forecasted in relative values and the privacy of the money issue is being maintained.

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